

Corrections

for

**Functions of One Complex Variable, II**

by

John B Conway

This is a list of corrections for my book Functions of One Complex Variable, II. This is also available from my WWW page (<http://www.math.utk.edu/~conway>).

Thanks to R B Burckel.

**I would appreciate any further corrections or comments you wish to make.**

**Minor corrections**

<b>Page</b>	<b>Line</b>	<b>From</b>	<b>To</b>
ix	10	built in	built-in
3	22	$\sum_{j=1}^m n(\gamma; a) = 0$	$\sum_{j=1}^m n(\gamma^j; a) = 0$
7	11	$\frac{\partial f}{\partial z} = \frac{1}{2} \left( \frac{\partial f}{\partial x} - i \frac{\partial f}{\partial y} \right)$ .	$\frac{\partial f}{\partial \bar{z}} = \frac{1}{2} \left( \frac{\partial f}{\partial x} + i \frac{\partial f}{\partial y} \right)$ .
13	18	Area( $D_n \cap G_k$ )	Area( $f(D_n) \cap \Lambda_k$ )
15	16	$u_x y$	$u_x dy$
22	-2	analytic	analytic
23	7	approach a	approach a
24	18	$\epsilon$	$\varepsilon$
24	-2	$\epsilon$	$\varepsilon$
25	23	approaches	approach
25	-13	free analyticity	free analytic
25	-10	analytically	analyticity
25	-7	$h(0) = 0$	$h(0) = a$
25	-5	$\pi/2 < \arg(z - r) < \pi/2 + \alpha$	$\pi/2 - \alpha < \arg(z - t) < \pi/2 + \alpha$
32	7	$f(B(b; \epsilon))$	$f(B(a; \varepsilon))$
33	11	bound region	bounded region
34	-7	$\setminus X_n$	$\setminus \tau(X_n)$
37	17	Schwartz	Schwarz
51	15	Jordan region	simple Jordan region
51	17	Jordan	simple Jordan
51	-4	Jordan	simple Jordan
53	12	Jordan	simple Jordan
54	11	$= \left  \int_{\theta_1}^{\theta_2} \tau'(-1 + re^{i\theta}) r i e^{i\theta} d\theta \right $ .	$\leq \int_{\theta_1}^{\theta_2}  \tau'(-1 + re^{i\theta})  r d\theta$ .
54	12	the angle	the largest angle
54	12	$1 + re^{i\theta}$	$-1 + re^{i\theta}$
54	14	Schwartz	Schwarz
55	-18	Jordan	simple Jordan
56	-10	polynimally	polynomially
67	14	$\leq$	$\geq$
67	15	$\leq$	$\geq$
69	-18	(7.5)	(1.4)
69	-2	$a_n \geq g^{(n)}(0)/n!$	$ a_n  \geq  g^{(n)}(0) /n!$
71	-9	G	<i>G</i> (italics)
71	-7	the j's and k's here should be slanted.	
77	3	$\phi_1(\partial \mathcal{D}), \phi_1(\partial \mathcal{D}) = \phi_1(\partial K_{00})$	$\phi_1(\partial \mathcal{D}) = \phi_1(\partial K_{00})$
81	-7	$\{\Phi_0, \Phi_1, \dots, \Phi_n\}$	$\Phi_0, \Phi_1, \dots, \Phi_n$

82	-3	Thus there are Jordan arcs	Since $C_j$ is an analytic curve, there are Jordan arcs
83	1	value	value
82	-2	$\eta_1(0) \neq \eta_2(0)$ ,	$\eta_1(0) \neq \eta_2(0),  \eta_i(t) - a_i  < \varepsilon$ ,
83	5	and $\text{ins } C \subseteq G$	and $C \subseteq \{z \in G : \text{dist}(z, C_j) < \varepsilon\}$ , so $\text{ins } C \subseteq G$
83	8	such that $\phi(\text{ins } C) = \text{ins } \gamma$	such that $\phi(\text{ins } C) \subseteq \text{ins } \gamma$
84	3	$(z - a)^{-1}$	$(z - \alpha)^{-1}$
84	-1	multiplicities	multiplicities
85	9	$C$	$\mathbb{C}$
85	18	set is non-empty	set contains 0
91	11	that is insistent on	that requires
91	-8	inner circle of $\Omega$ .	inner circle of $\Omega$ and orient $\gamma_1$ so that $n(\phi(\gamma_1); 0) = -1$ .
92	13	with $\psi$ .	with $\psi$ . Since $f$ is a conformal equivalence we have $n(\psi(\gamma_1); 0) = n(f(\phi(\gamma_1)); 0) = -1$ .
92	-5	So $n(\gamma_1; 0) = -1$ , $n(\gamma_0; 0) = 1$ , and $n(\gamma_j; 0) = 0$ for $2 \leq j \leq n$ .	So $n(\gamma_j; 0) = 0$ for $2 \leq j \leq n$ and we can orient $\gamma_0$ and $\gamma_1$ such that $n(\gamma_1; 0) = -1$ and $n(\phi_0; 0) = 1$ .
93	11	analytic Jordan	analytic $n$ -Jordan
94	3	Argument Principle	Argument Principle, if $\zeta \notin \phi(\gamma_j)$ for $0 \leq j \leq n$ , then
94	8	that $0 \leq j \leq n$ and $ \zeta  \neq r_j$ ,	that for $0 \leq j \leq n$ ,
97	-11	$f : G \rightarrow \Lambda$	$f : \Omega \rightarrow \Lambda$
98	-2	$n(\gamma_j, a)$	$n(\gamma_j; a)$
101	-12	$\frac{r_j^2}{\bar{z} - \bar{a}_j}$	$\frac{r_j^2}{\bar{z} - \bar{a}_j}$
102	-8	(14.7.14)	(14.7.16)
103	-13	$\sum_{k=m}^n$	$\sum_{k=m}^{\infty}$
106	10	It follows that $g(\mathbb{D}) = \mathbb{D}$ and so $g(z) - \lambda(z - a)(1 - \bar{a}z)^{-1}$ .	It follows from Proposition 7.5 that $g$ is a Möbius transformation.
107	16	theorem.	theorem.
107	-14	equivalence	equivalences
110	20	$z \in T(w)$	$z \in T(W)$
110	-4	bet	be
113	-2	$(G, \tau)$	$(G_1, \tau_1)$
114	-5	But the only way such a conformal equivalence can exist is if $G = \mathbb{C}$ . But then Proposition 14.1.1 implies	But according to Proposition 14.1.1, $G = \mathbb{C}$ and $h(z) = az + b$ for complex numbers $a$ and $b$ with $a \neq 0$ .

		that $h(z) = az + b$ for complex numbers $a$ and $b$ with $a \neq 0$ .	
116	10	dentoed	denoted
119	10	$\text{Im } z = \text{Im } M^{-1}M(z) <$	$\text{Im } z = \text{Im } MM^{-1}(z) < \text{Im } M^{-1}(z)$
			$\leq \text{Im } z$
119	-10	$c, d \in \mathbb{Z}$	$c, d \in \mathbb{Z}$ and $c, d$ occur in some $M$ in $\mathcal{G}$
119	-7	$G$	$\mathcal{G}$
121	10	an	and
122	5	no common divisor, there is an odd integer $d$ such that $b$ and $d$ have no common divisor and there is an odd integer $a$	no common divisor, there is an odd integer $a$
122	-14	a neighborhood of $z_+$ and	an open neighborhood of $z_+$ (Verify!) and
122	-4	First $\lambda$	First, $\lambda$
124	6	Proposition 2.1	Theorem 1.3 and Proposition 2.1
124	15	$\mathcal{F} B$	$\mathcal{F} B$
124	-7	$w$ in $B$	$z$ in $B$
126	15	continuation	continuation along $\gamma$
126	18	continuation and	continuation, $g_i(\Delta_i) \subseteq G$ , and
126	20	$(G_n, \Delta_0)$ ,	$(G_n, \Delta_0)$ and $g(\Delta) \subseteq G$ ,
126	-9	path $\gamma$	path $\gamma$ such that $g_t(\Delta_t) \subseteq G$ for all $t$
126	-8	$z$ in $\Delta_t$	$z$ ( <i>italics</i> ) in $\Delta_t$
127	2	neighborhood of $\alpha_0$	neighborhood of $\alpha_0$ that is contained in $\Omega$
127	5	$g(\alpha_0)$ and	$g(\alpha_0) = 0$ and
127	7	continuation	continuation along $\gamma$
127	8	that $g_t(\Delta_t)$	that $\Delta_t \subseteq \Omega$ and $g_t(\Delta_t)$
127	10	continuation and	continuation with $\Delta_i \subseteq \Omega$ and
127	15	Since $h_0 \in \mathcal{F}$ , $\mathcal{F} \neq \emptyset$ .	Hence $h_0 \in \mathcal{F}$ and $\mathcal{F} \neq \emptyset$ .
127	-16	$B(\alpha_0; \delta)$	$B(\alpha_0; \delta)$
128	8	the function	a function
128	12	continuation of $h$ ever	continuation of $h$ in $G$ with values in $\mathbb{D}$ ever
128	-8	$g'(h(\alpha_0))\kappa$	$g'(h(\alpha_0))\kappa$
129	4	the function	a function
129	19	Thus the	Thus (there is something extra to do here) the
129	-7	approches	approches
131	-7	$f(a) = 0$	$f(a) = a$

$$205 \quad -10 \quad \operatorname{Re} \left( \frac{1 + \bar{w}}{1 - z\bar{w}} \right)$$

$$\operatorname{Re} \left( \frac{1 + z\bar{w}}{1 - z\bar{w}} \right)$$

### More substantial corrections

#### Page Line From

13 14 Because  $f(\partial D_n)$  is a smooth curve,

82 20 Theorem 3.4 should also show that if  $G$  is on the “left” of a boundary curve  $\gamma$  of  $G$ , then  $\Omega$  is on the “left” of  $\phi(\gamma)$ .

136 -8 **Add the following sentence as a separate paragraph.**

The treatment in this section and the next are based on Duren [1983].

385 In the appropriate place, add the following reference.

P L Duren [1983], *Univalent Functions*, Springer-Verlag, New York.

#### To

The set  $G \setminus \cup_n D_n$  can be written as a countable union of compact sets  $\cup_j K_j$  (Why?). Since  $f$  is analytic and locally Lipschitz. Thus Area  $f(K_j)$  for each  $j \geq 1$ . Thus